Day 28

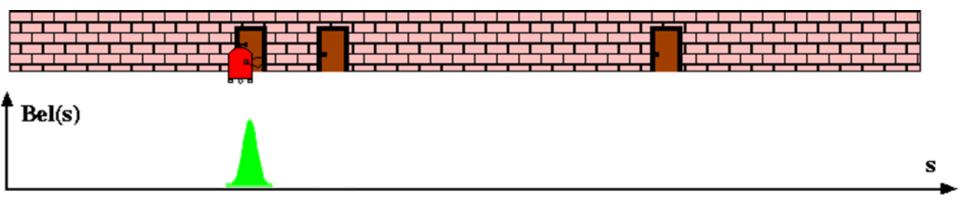
Non-parametric Filters

Localizing a Robot in a Hallway

- consider a robot moving down a hall equipped with a sensor that measures the presence of a door beside the robot
 - the pose of the robot is simply its location on a line down the middle of the hall
 - the robot starts out knowing how far down the hallway it is located
 - Kalman-like filters require an initial estimate of the location
 - robot has a map of the hallway showing it where the doors are

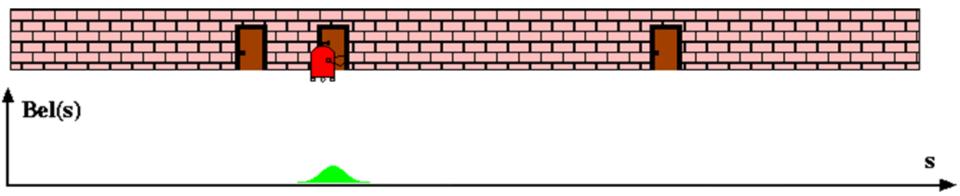
Kalman Localization

robot starts out knowing how far down the hallway it is located

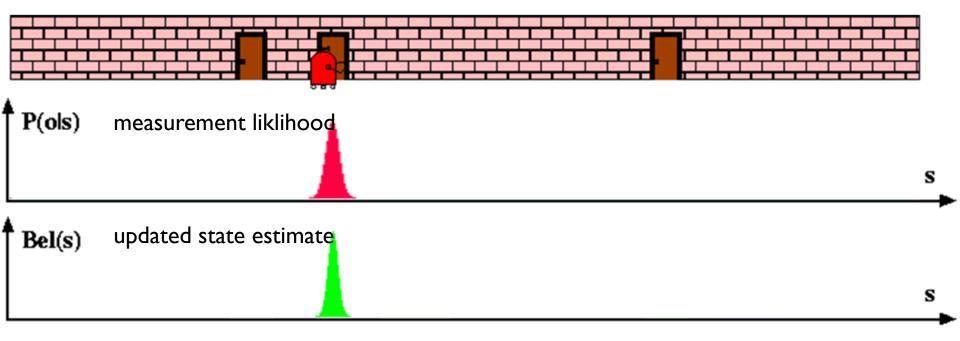


Kalman Localization

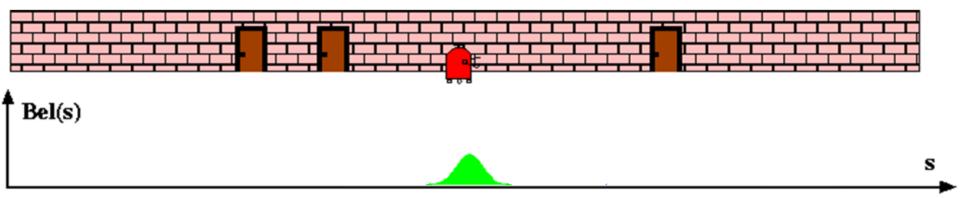
as the robot moves forward, its uncertainty in its location shifts and grows according to its motion model



when it reaches a door that can be uniquely identified, it can incorporate this measurement into its state estimate

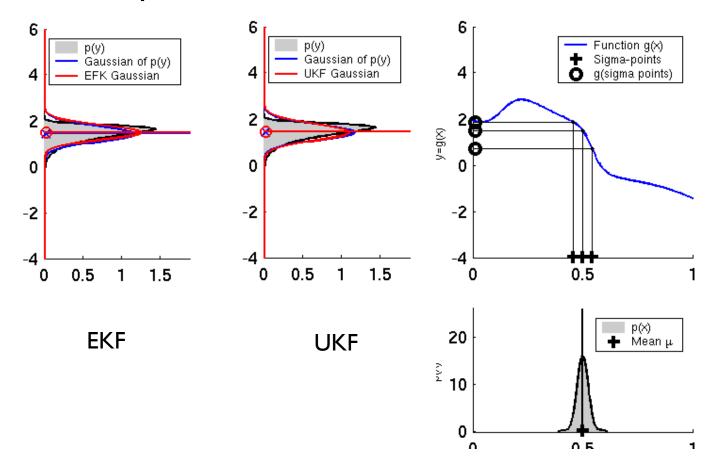


as the robot moves forward, its uncertainty in its location shifts and grows according to its motion model

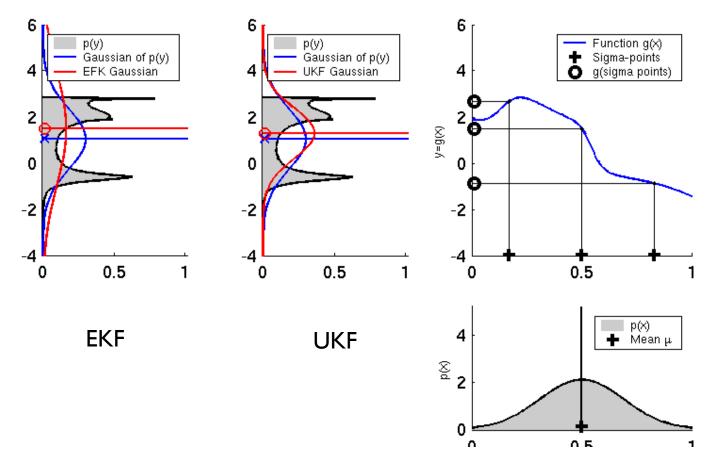


- Kalman-like filters assume that quantities can be represented accurately as a mean + covariance
 - e.g., the state is a random variable with Gaussian distribution
 - e.g., measurements are random variables with Gaussian distribution

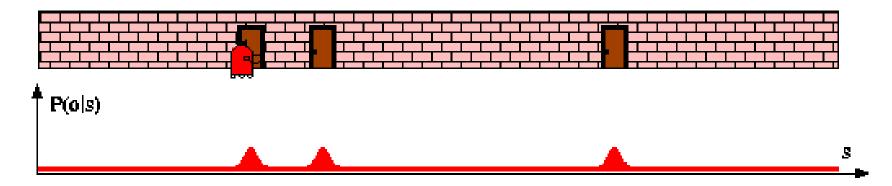
assumption is ok here



assumption is (possibly) not ok here



 assumption is not ok here (robot does not know which door it is measuring)



p(x | robot is sensing a door)

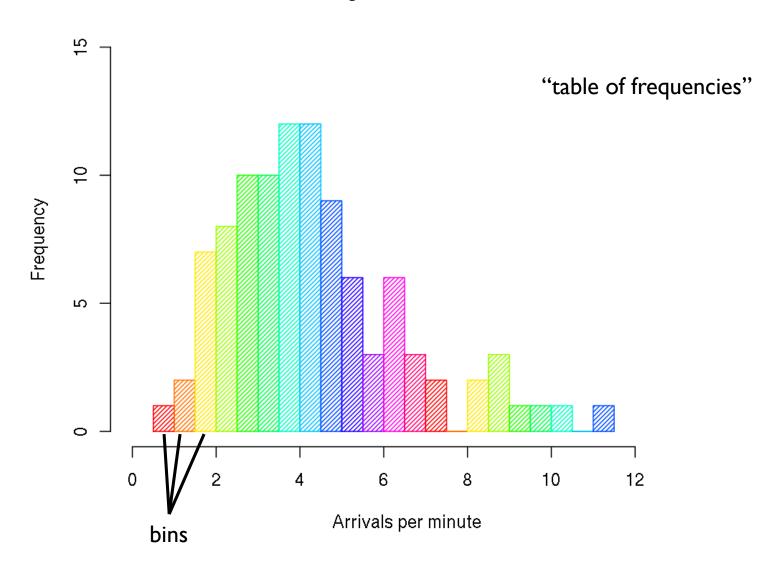
Non-parametric Filters

- non-parametric filters do not rely on a fixed functional form of the state posterior
- instead, they represent the posterior using a finite number of values each roughly corresponding to a region (or point) in state space
- two variations

- I. partition state space into a finite number of regions
 - e.g., histogram filter
- 2. represent the posterior using a finite number of samples
 - e.g., particle filter

Histogram

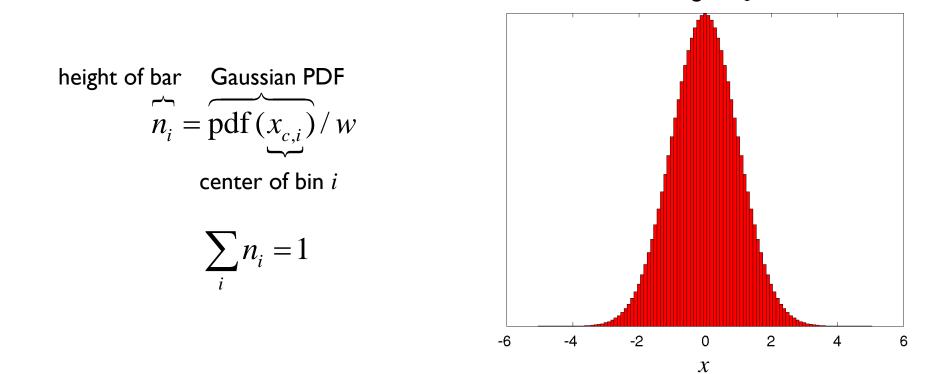
Histogram of arrivals



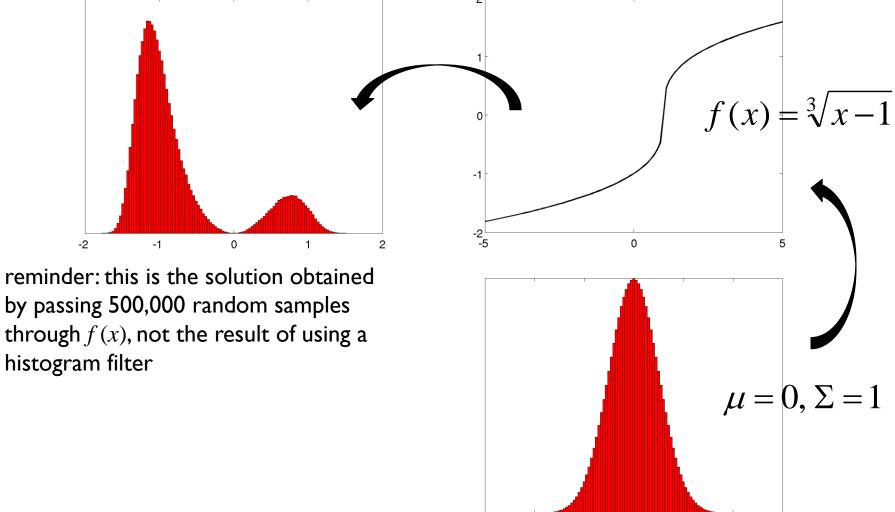
- histogram filter uses a histogram to represent probability densities
- in its simplest form, the domain of the densities is divided into subdomains of equal size with each subdomain being a bin of the histogram
 - the value stored in the bin is proportional to the density

- suppose the domain of the state x is [-5, 5] and that x is a random variable with Gaussian density (mean 0, variance 1)
 - using bins of width w = 0.1 we can represent the density using the following histogram

histogram p



suppose we want to pass the density through some non-linear function



-6

-2

2

4

6

3/22/2017

0

- 1. create an empty histogram h with bins $x_{c,i}$
- 2. for each i
 - $I. \quad y_i = f(x_{c,i})$
 - $2. \qquad n_i = p(x_{c,i})$
 - 3. find the bin b_k that y_i belongs in
 - 4. $h(b_k) = h(b_k) + n_i$

A Simple Implementation

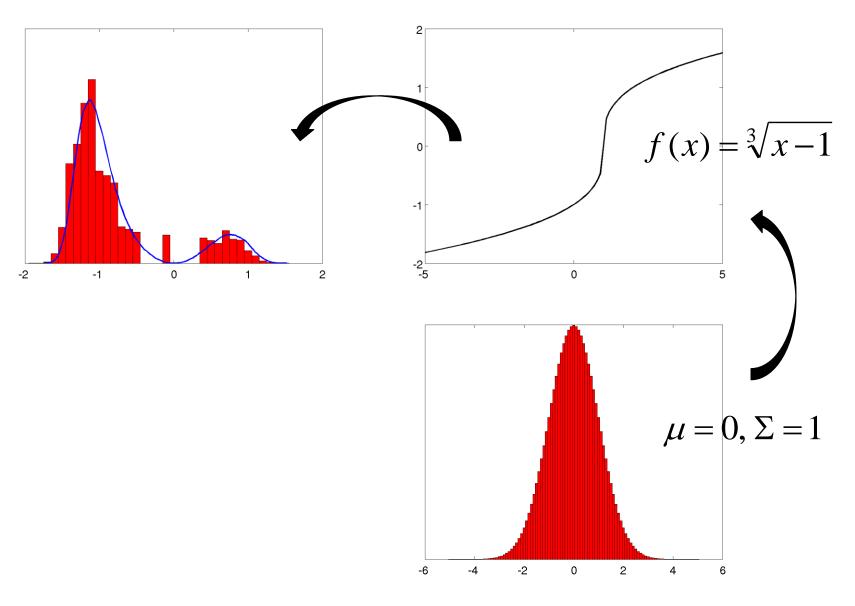
% width of x bins dx = 0.05;% bin centers x xc = -5:dx:5;y = nthroot(xc - 1, 3); % y = f(xc)n = normpdf(xc, 0, 1); % n = p(xc)% width of y bins dy = 0.1;yc = -2:dy:2;% bin centers y h = zeros(size(yc)); % histogram for i = 1:length(y)bk = find(y(i) > yc - (dy / 2) & y(i) < yc + (dy / 2));h(bk) = h(bk) + n(i);end bar(yc, h, 1);

- alternatively
- I. create an empty histogram h with bins $x_{c,i}$
- 2. for each bin b_k

1.
$$h(b_k) = \sum_i p(x_{c,i}) \text{ in bin } (y_i, b_k)$$

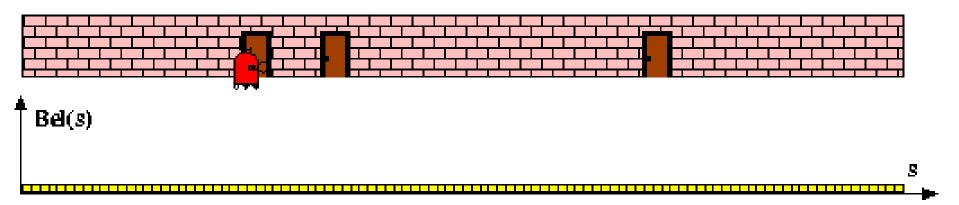
$$y_i = f(x_{c,i})$$

in_bin (y_i, b_k) probability that y_i is in bin b_k

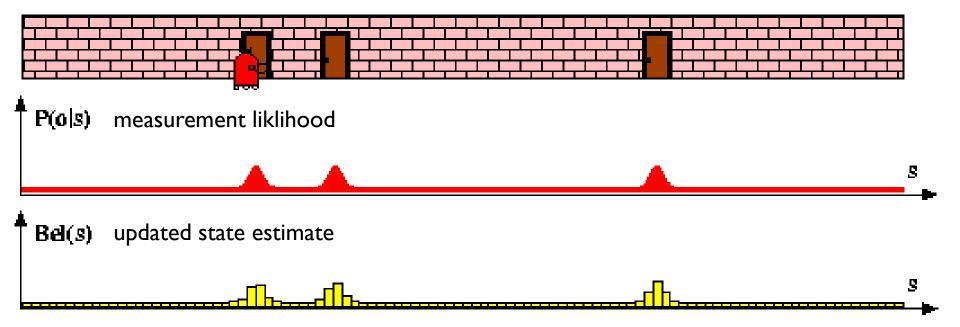


- grid localization uses a histogram filter over a grid decomposition of pose space
- consider a robot moving down a hall equipped with a sensor that measures the presence of a door beside the robot
 - the pose of the robot is simply its location on a line down the middle of the hall
 - the robot starts out having no idea how far down the hallway it is located
 - robot has a map of the hallway showing it where the doors are
 - grid decomposes the hallway into a finite set of non-overlapping intervals
 - e.g., every 50cm would yield intervals [0, 0.5], (0.5, 1], (1, 1.5], ...

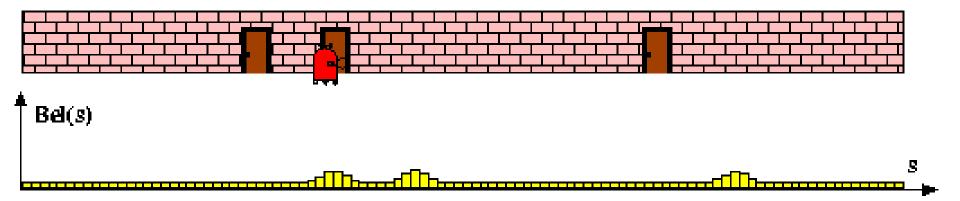
- the robot starts out having no idea how far down the hallway it is located
 - the histogram of its state density is uniform



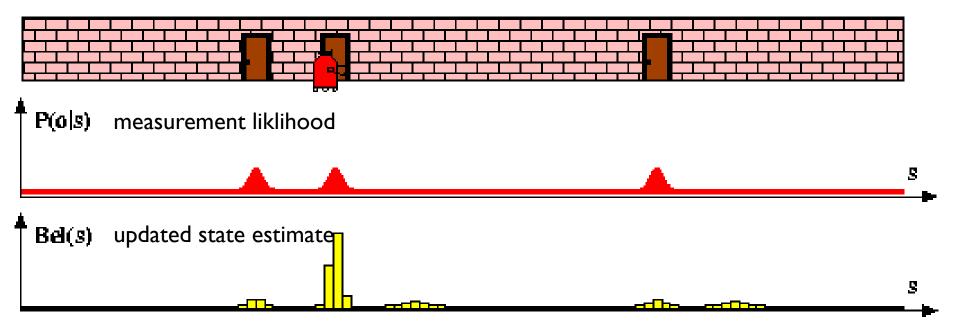
- because the robot is beside a door, it has a measurement
 - it can incorporate this measurement into its state estimate



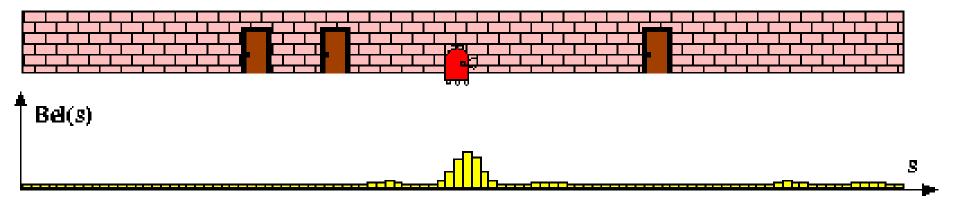
as the robot moves forward, its uncertainty in its location shifts and grows according to its motion model



- when it reaches a door, it can incorporate this measurement into its state estimate
 - > it now has a pretty good idea where it is in the hallway



as the robot moves forward, its uncertainty in its location shifts and grows according to its motion model



Grid Localization Algorithm

- I. algorithm_grid_localization($\{p_{k,t-1}\}, u_t, z_t, m$)
- 2. for all k do
- 3. $\overline{p}_{k,t} = \sum_{i} p_{i,t-1} \text{ motion_model}(\text{ mean}(\mathbf{x}_k), u_t, \text{ mean}(\mathbf{x}_i))$ 4. $p_{k,t} = \eta^i \overline{p}_{k,t} \text{ measurement_model}(z_t, \text{ mean}(\mathbf{x}_k), m)$
- 5. endfor
- 6. return $\{p_{k,t}\}$

$\{p_{k,t}\}$	histogram
\mathcal{U}_t	control input
Z_t	measurement
т	map
$mean(\mathbf{x}_i)$	center of mass of grid cell \mathbf{x}_i